



GNC description and result synthesis

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Summary

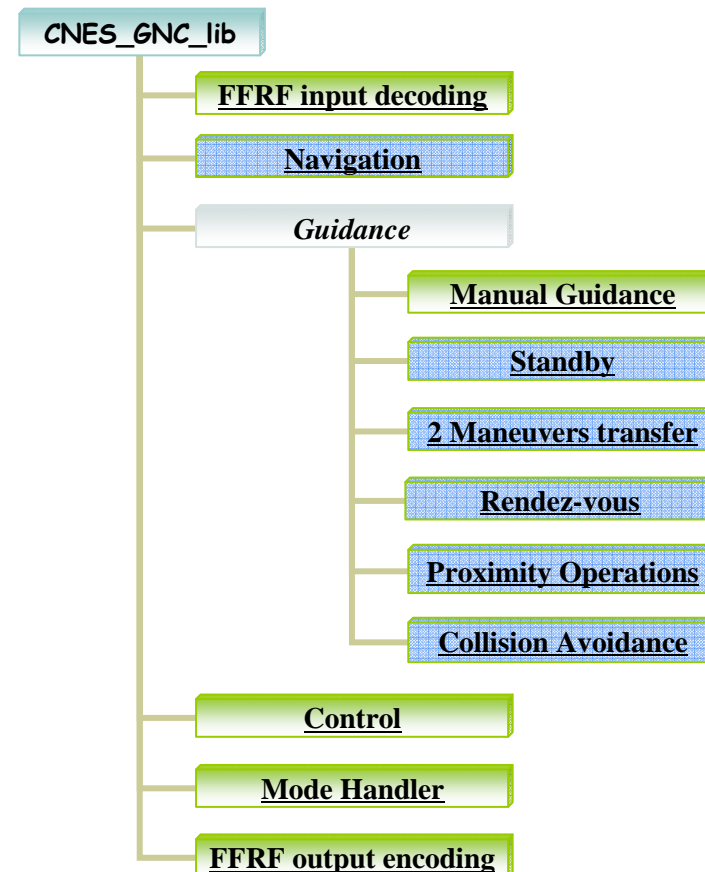
- **Nominal mission**
 - ♦ Algorithms
 - ♦ Results synthesis

- **Extended mission**
 - ♦ Algorithms
 - ♦ Results synthesis

- **GNC results summary**



- 11 functions integrated within CNES_GNC_lib
- 6 guidance functions, each one dedicated to a Formation Flying experimental phase
- Distribution oriented towards:
 - ♦ Experimental objectives
 - ♦ Easy validation and development of each function



GNC Activity	Number of occurrences	Duration
RF Navigation	Continuously	12 days CL 40 days OL
Standby	4 nominal SBY	2.5 days
	1 with autonomous transfer in case of anomaly	
Proximity operations	7 sessions	2 days
Rendezvous	6 nominal RDV with distances up to 9 km	4 days
	1 reverse RDV	
N* 2 manoeuvres transfer	11 simple 2MT	1 day
	2 multi-orbits 2MT	
Collision avoidance	2 double boosts ("Soft" CA)	2 days
	4 single boost ("Drift" CA)	

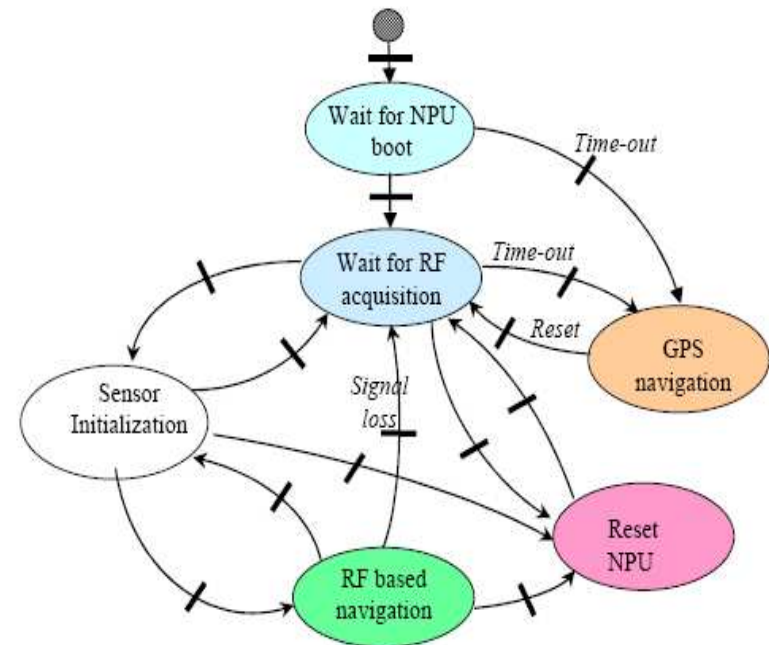
12 closed loop days
5.72 m/s delta-V consumption
3 à 4 switch modes / day

GPS post-processed data by POD-DLR
(Precise Orbit Determination) used as
reference to performance evaluation

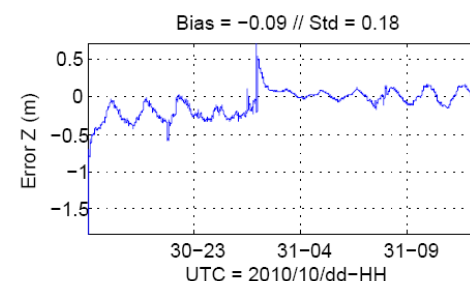
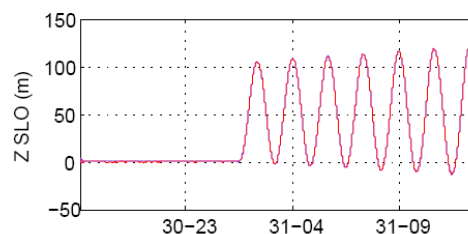
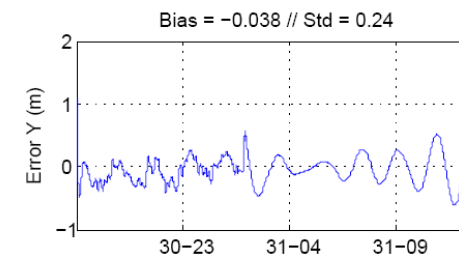
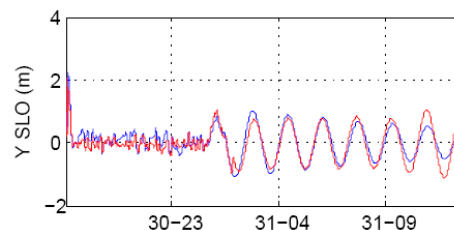
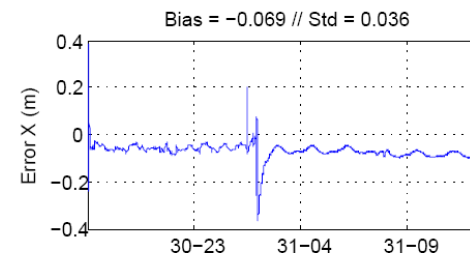
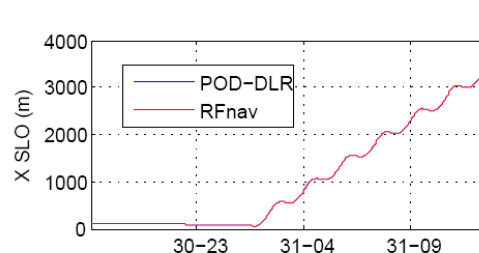


3 main functional blocks / 6 different sub-modes of operation :

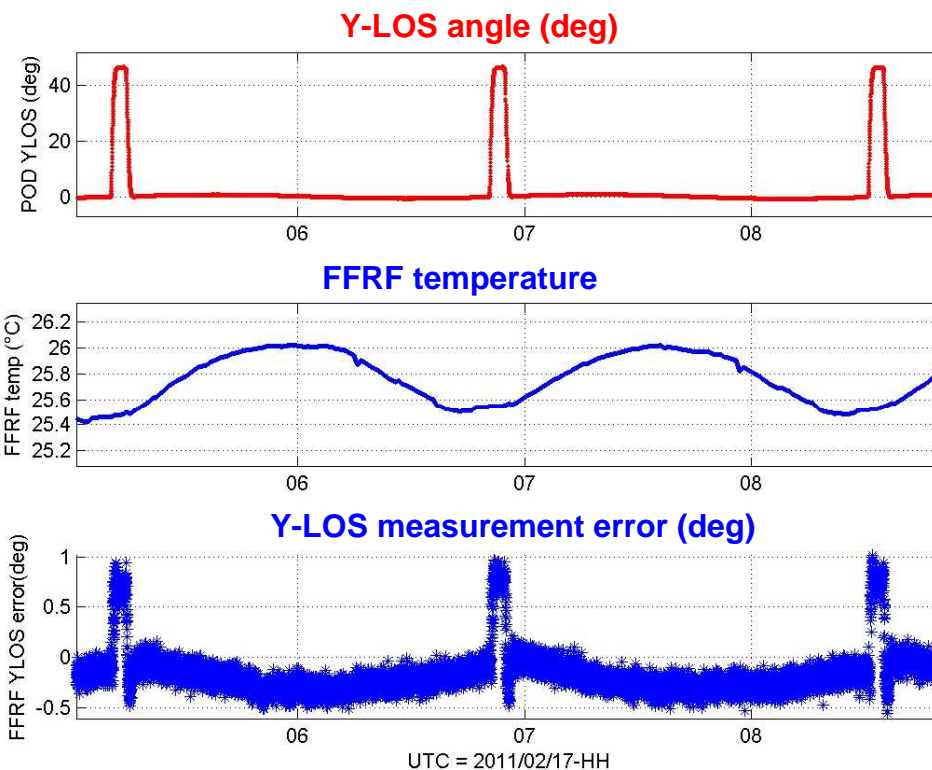
- ♦ Estimation of MANGO relative state (in TANGO Local Orbital Frame):
 - Extended Kalman Filter to estimate 8 state : 3 for the position, 3 for the velocity and 2 for Light of Sight FFRF bias
- ♦ Calculation of the Local Orbital Frame (attached to the TARGET):
 - propagating the Tango S/C state taking into account external forces (J2, drag and solar pressure). Absolute state updated by the ground on a regular basis.
- ♦ Management of FFRF sensor:
 - Computing aiding data,
 - Monitoring FDIR (NPU reset) mechanism



- Provides aid during Initialization (IAR)
- Typical convergence time = 3000s for LOS bias estimation
- Performance depends on relative range and manoeuvre frequency
 - ◆ Best performance achieved during PROX activities: a few cm error
 - ◆ Range impact is particularly visible during RDV and separation after CAM : a few m error in cross track



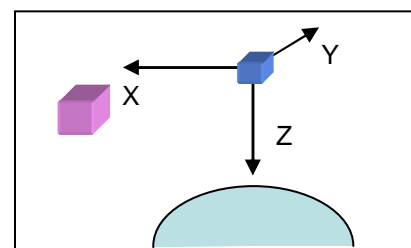
- Most important error source is LOS bias variation :
 1. Multipath during attitude manoeuvres
 2. FFRF temperature evolution
- 1st effect mitigated by covariance adaptation during large manoeuvres
- 2nd effect mitigated by a specific attitude programming



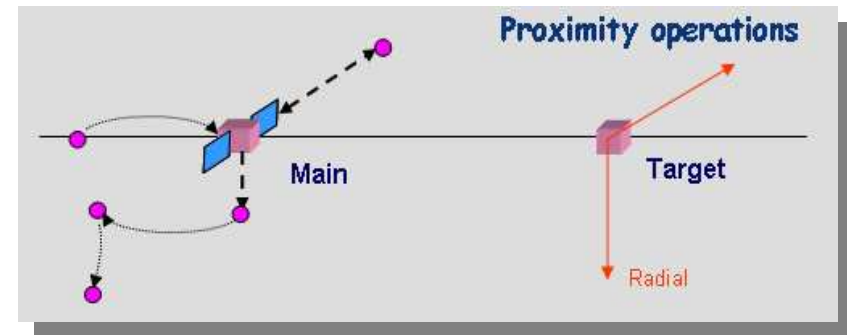
Mode	Inter satellite Distance (ISD)	Error in position estimation in SLO (cm) frame	Error in bias LOS estimation (deg)
RDV	4000 – 200 m	Bias [5.7 24 0.9] Std [1.7 350 7.4]	Bias [0.0016 0.0039] Std [0.009 0.091]
CA	60 – 4200 m	Bias [8 -1.3 2.1] Std [3.5 27 10]	Bias [0.002 -3e-4] Std [0.037 0.037]
SBY	60 - 140 m	Bias [-31 2.3 1.0] Std [3.0 13.0 5.5]	Bias [-0.0022 0.0023] Std [0.038 0.093]
PROX	20 m	Bias [-2.8 1 5.7] Std [0.6 1.4 1.7]	Bias [0.16 0.028] Std [0.050 0.039]

Reduced crosstrack accuracy

centimetric accuracy



Maintain MANGO on a hold point and / or forced translation (following the 3 axis) :



«Guidance» component :

- ♦ Calculation of references linear trajectories between two hold points.

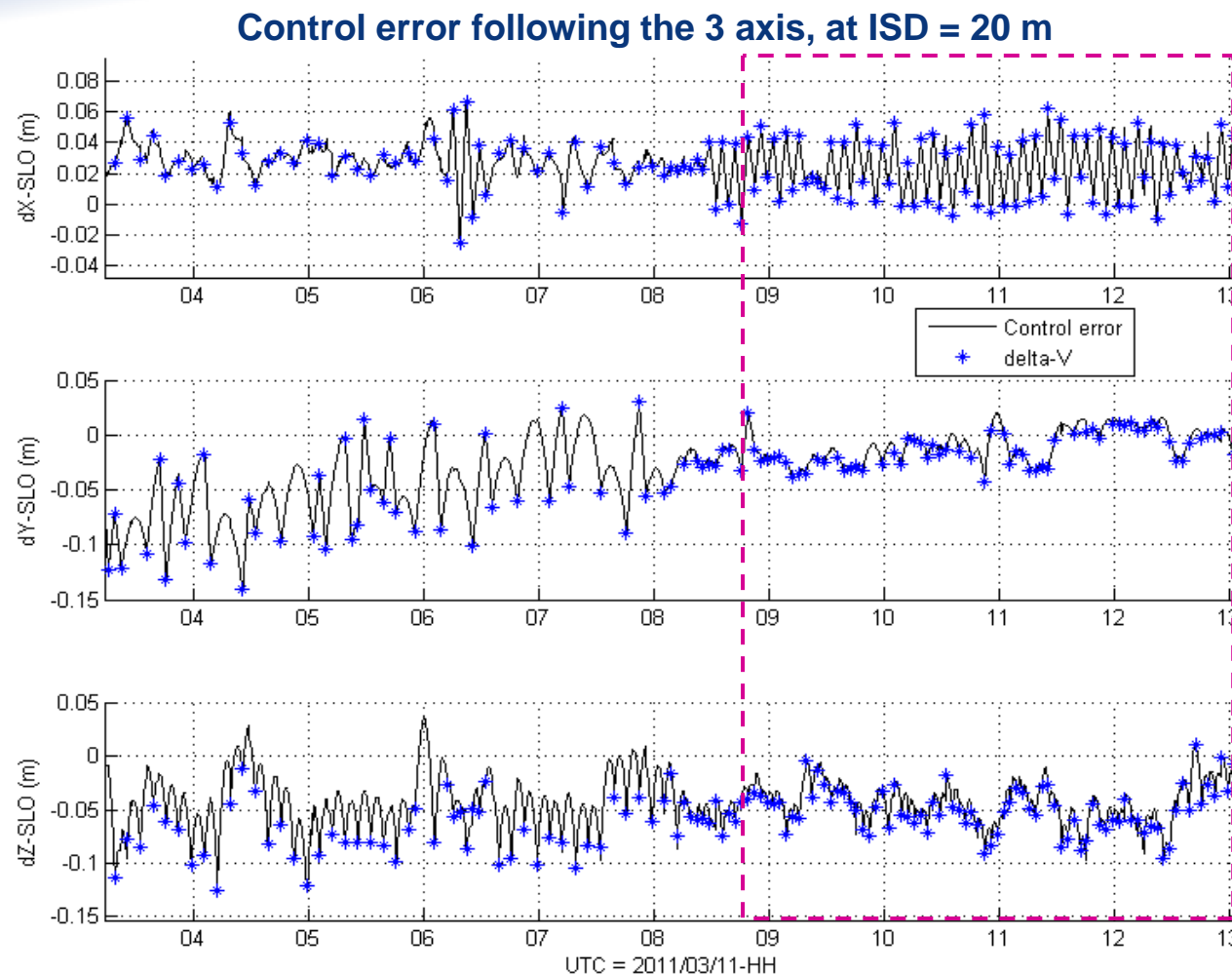
«Control» component :

- ♦ Periodic dV computation to follow the reference trajectory,
- ♦ Linear Quadratic Regulator (LQR) control,
- ♦ Control gains pre-computed on ground (Clohessy-Wiltshire model),
- ♦ «Feed forward» M gains to take into account some perturbations : drag and solar pressure
- ♦ Control period : [100s , 400s]

■ Impact of the thrusters frequency (MIB = 0.4 mm/s)

■ Improving accuracy

■ dV consumption :
3 cm/s/orbit
↓
5 cm/s/orbit



Thrusters operating in a differential way

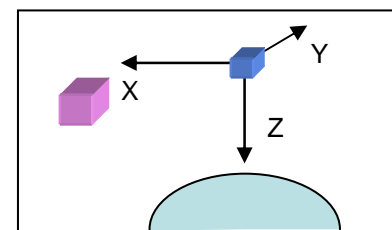


Error due to
control part only

Closed-loop global
error

Activity	Navigation error (cm) POD as Ref	Control accuracy (cm) RF nav as Ref	Control accuracy (cm) POD as Ref
80m SK no sub-pulse	Bias = [-3.7 -11 5] Std = [0.5 4.7 5.4]	Bias = [0.1 0.6 1.6] Std = [1.8 2.5 3.2]	Bias = [3.8 12 -3.4] Std = [1.8 5.7 6.7]
80m SK with sub-pulse	Bias = [-3.5 -15 14] Std = [0.5 3.4 3.3]	Bias = [-0.1 -0.1 0.9] Std = [0.9 1.8 1.6]	Bias = [3.4 14 -13] Std = [0.9 4.1 3.5]
20m SK no sub-pulse	Bias = [-2.7 6.2 5.4] Std = [0.6 2.2 1.8]	Bias = [0.2 1.3 1.1] Std = [1.1 2.3 2]	Bias = [2.9 -4.7 -4.3] Std = [1.1 3.6 2.7]
20m SK with sub-pulse	Bias = [-2.8 1 5.7] Std = [0.6 1.4 1.7]	Bias = [-0.4 -0.1 1.4] Std = [1.1 0.7 0.8]	Bias = [2.4 -1.1 -4.3] Std = [1.3 1.5 1.9]

Contributor : intrinsic POD error (on Xslo)
whose standard deviation amplitude is around
6 mm (comparison with the FFRF distance
whose noise is much lower than that)

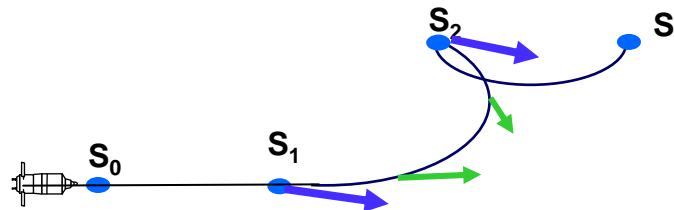


Nominal Mission : GNC functions

2 Maneuvers transfer function

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- **Description** : Transfer between 2 MANGO relative positions via 2 impulsive maneuvers (Similar than Far RdV ATV)



■ Relative dynamic modelisation:

- ♦ Tschauner-Hempel equations=> Yamanaka-Ankersen STM (take into account eccentricity) + curvilinear correction of relative positions and velocities

■ Two impulsive maneuvers : $\{t_0, \Delta V\}$ et $\{t_f, \Delta W\}$

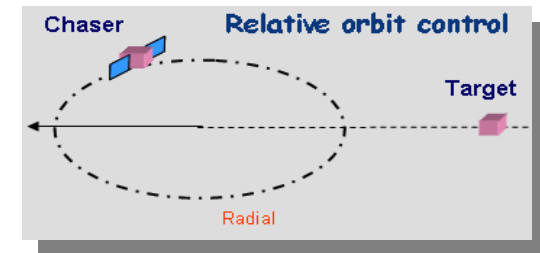
- ♦ Linear system inversion (on board) : 6 equations , 6 unknowns
- ♦ Addition of trim maneuvers and way-point target

Nominal Mission: 2MT

Theoretical Conditions: Initial Position Final Targeted Position (m)	Transfer Duration (orbits)	Delta-V consumption (cm/s)	Number of manoeuvres	Transfer accuracy (m and mm/s) POD as Ref
330 m → 600 m	0.75	3.6	4	3.72 m / 25.0 mm/s
500 m → 100 m	0.75	12.3	4	1.08 m / 18.58 mm/s
500 m → 260 m	1.75	14.2	5	1.75 m / 3.41 mm/s
-100 m → -30 m	0.70	2.7	4	1.0 m / 4.94 mm/s

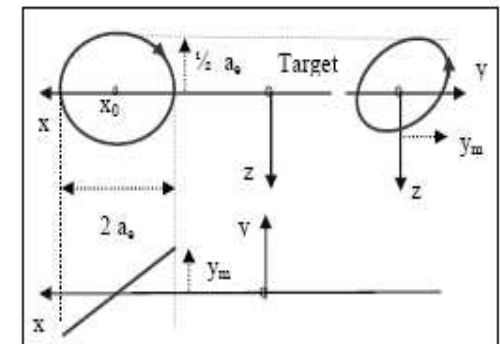
■ Description:

- ♦ Maintain MANGO on a stable relative orbit during “stand-by” phases (nominal mode), with minimizing dV consumption,
- ♦ After an anomaly, retreat to a stable relative orbit whatever MANGO initial states (retreat mode), with minimizing dV consumption



■ Relative dynamic modelisation:

- ♦ Tschauner-Hempel equations => Yamanaka-Ankersen STM (take into account eccentricity) + curvilinear correction of relative positions and velocities relatives
- ♦ MANGO maintained on a stable « football » orbit

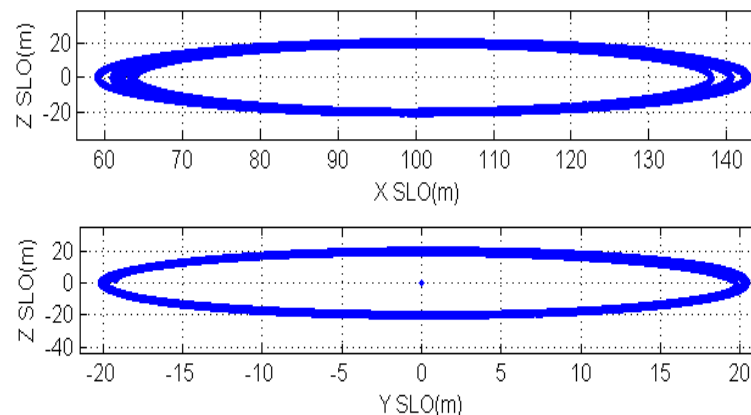


■ Maneuvers control :

- Periodic control using 2-maneuver transfer
- Decoupled in-plane and out-of-plan motion => decoupled control
- Optimization of “retreat” maneuver (destination in case of “soft” anomaly)

- 3 slots in normal mode – few orbits
- 1 slot in recovery mode for in-flight anomaly recovery scheme qualification
- 1 slot in normal mode -1.5 day - to asses long term performance and the link between orbital position and orbit maintenance cost

→ 40 orbits for an overall cost of 6.86 cm/s ie 1.7 mm/s/orbit



	Mean control error (1 sigma)	
	x0 (m)	ym (m) ym_ref = 20m
x0ref = 300m, ~3 orbits	1.36 (2.16)	0.61 (0.24)
x0ref = 300m, ~5 orbits	5.27 (2.91)	0.56
x0ref = -200m, ~3 orbits	-5.18 (1.64)	- (0.13)
x0ref = 102m, ~7 orbits (recovery)	-0.56 (1.57)	0.16 (0.14)
x0ref = 300m, ~20 orbits	-3.04 (2.2)	-0.34 (0.27)

Mean bias = 3 m
Mean sigma = 2m

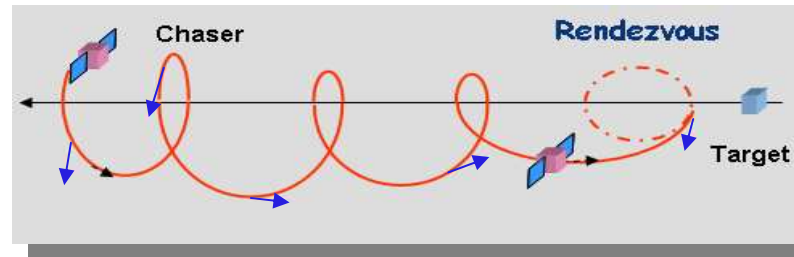
Mean bias = 0.3 m
Mean sigma = 0.2 m



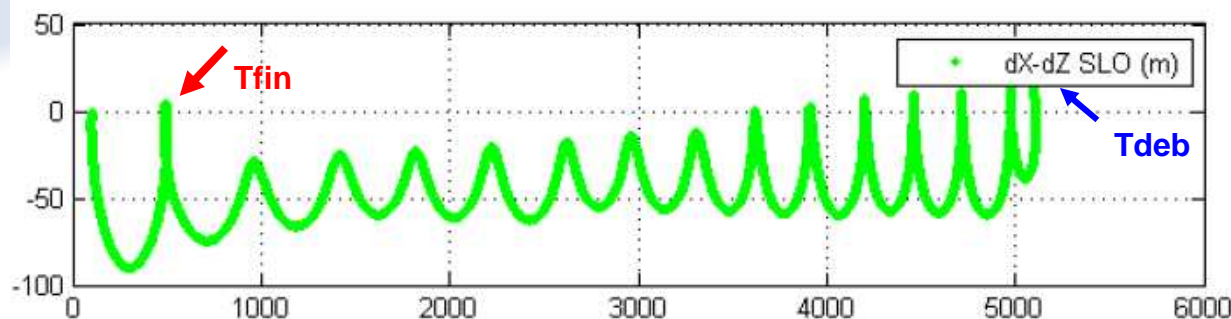
Nominal Mission : GNC functions

Rendezvous function

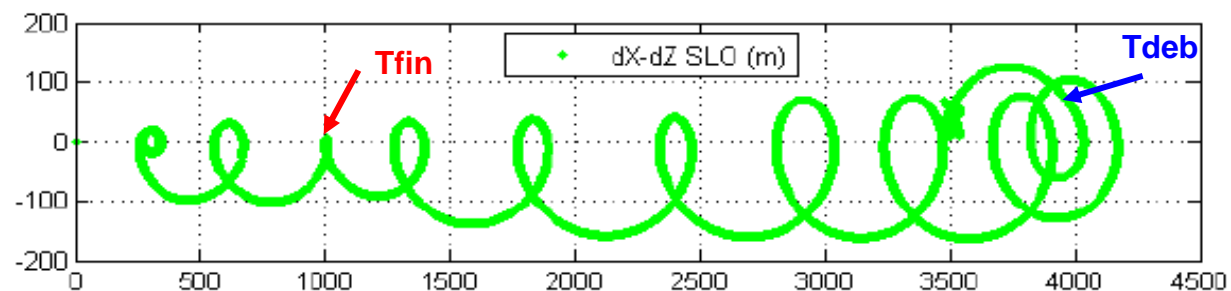
- **Description:** Rendezvous (or deployment) between MANGO current position and the vicinity of a target point:



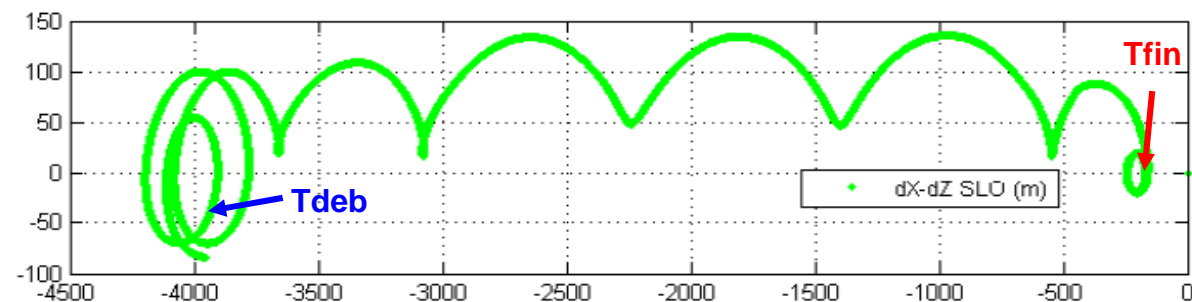
- **Relative dynamic modelisation:**
 - ♦ Tschauner-Hempel equations => Yamanaka-Ankersen STM (take into account eccentricity) + curvilinear correction of relative positions and velocities relatives
 - ♦ Linear time variant (LTV) state-space model
- **ΔV optimization:**
 - ♦ Maneuver plan : impulsive ΔV_k ($k \leq 10$) with fixed realization dates
 - ♦ Quadratic programming problem with linear equality constraints + feedback scheme based in MPC (Model Predictive Control) framework to update (on board) the maneuver plan,
 - ♦ Guidance Q_n matrices : pre-calculated on ground and then uploaded by TC



GNC1-1-b :
 $[5000, 0, 0] \Rightarrow [500, 0, 0]$
 Duration : 23 h 45 min
 10 Maneuvers



GNC1-2-b :
 $[4000, 5, 90] \Rightarrow [1000, 0, 0]$
 Duration : 13 h
 9 Maneuvers



GNC1-3-b :
 $[-3723, -1.4, -42] \Rightarrow [-160, 20, 0]$
 Duration: 13 h
 8 Maneuvers

Theoretical Conditions: Initial Position Final Targeted Position (m)	Rendezvous Duration (orbits)	Rendezvous accuracy (m and mm/s) RF nav as Ref	Rendezvous accuracy (m and mm/s) POD as Ref
5000 m → 500 m	14.25	2.49 m / 1.99 mm/s	1.40 m / 1.74 mm/s
170 m → 100 m	2	0.73 m / 0.68 mm/s	0.53 m / 3.57 mm/s
-3720 m → -160 m	7.8	0.73 m / 0.60 mm/s	0.25 m / 7.48 mm/s
6750 m → 500 m	6.8	2.60 m / 0.51 mm/s	1.72 m / 7.63 mm/s
-7200 → -2000 m	7.8	2.36 m / 1.18 mm/s	3.12 m / 9.78 mm/s

worst case @ 2 km
Position error : < 3.2 m
Velocity error : < 1 cm/s

RDV Requirements:
Position error : ≤ 50 cm
Velocity error : ≤ 1 cm/s



Nominal Mission: rendezvous operations dV consumption

Theoretical Conditions: Initial Position Final Targeted Position (m)	Monte Carlo simulations (cm/s)	Pre- computed on ground Delta-V (cm/s)	Delta-V on- board consumption (cm/s)
5000 m → 500 m	7.27 / 2.44	2.30	8.6 (x3.7)
4000 m → 1000 m	12.9 / 3.23	13.0	15.3 (x1.2)
170 m → 100 m	2.66 / 0.06	3.6	3.0 (x0.8)
-3720 m → -160 m	12.2 / 2.12	12.53	15.5 (x1.25)
6750 m → 500 m	n.a.	17.3	27.3 (x1.6)
-7200 m → -2000 m	n.a.	19.0	17.7 (x0.9)

Coherence between simus MC and
on flight results

Coherent additional cost with
others RDV projects



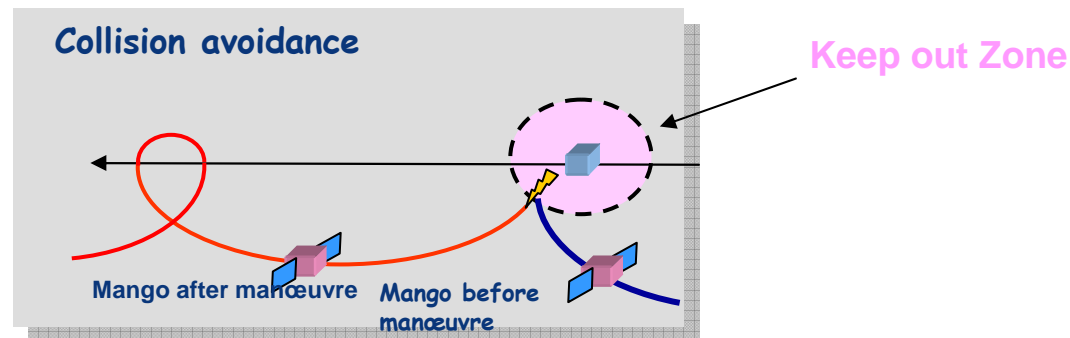
Nominal Mission : GNC functions

Collision Avoidance function

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■ Description:

- ♦ If collision risk is detected ($ISD < \text{threshold}$), collision avoidance algorithms shall compute a manoeuvre that sets the main spacecraft onto a relative orbit that remains outside the defined safety sphere, for a long enough period so that ground can hand over :



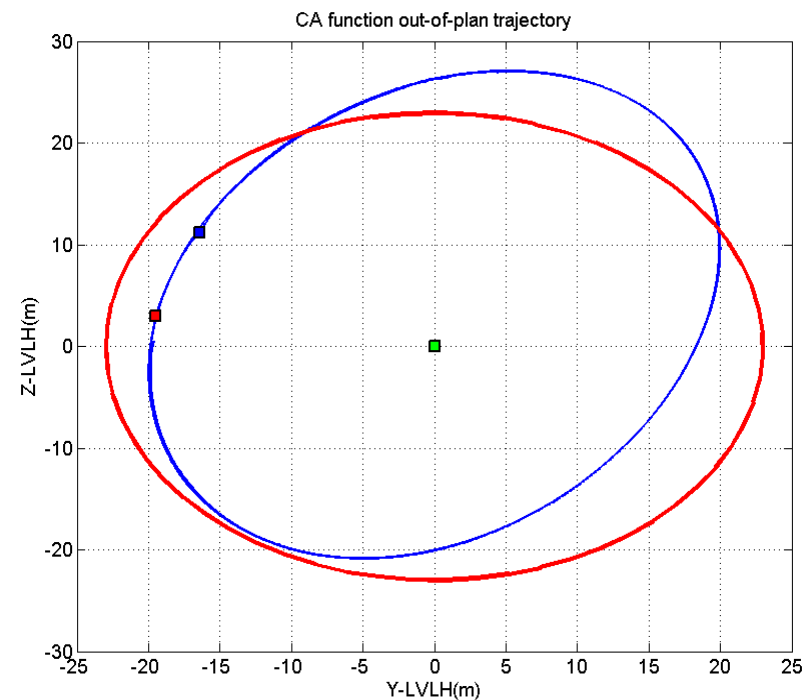
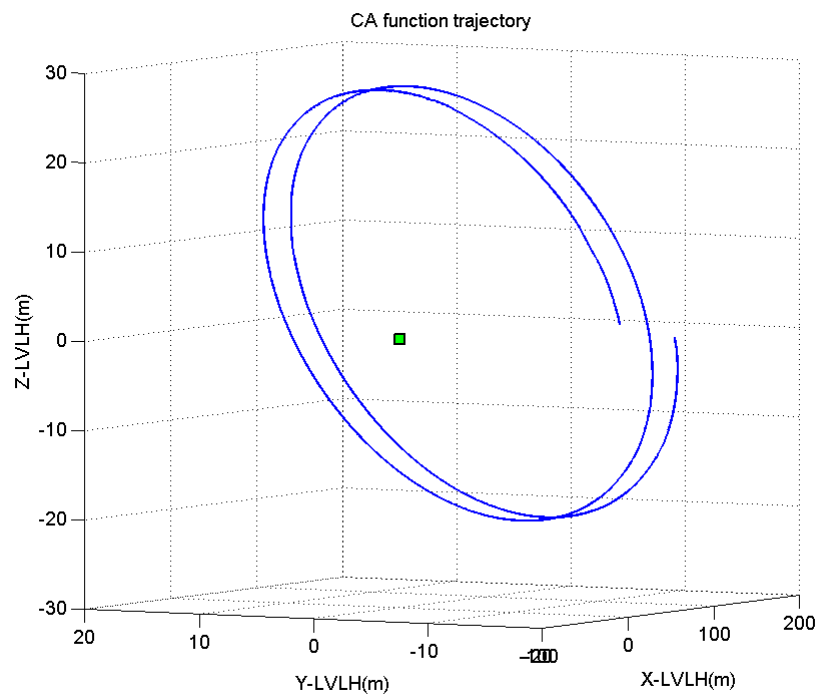
■ ΔV CAM :

- ♦ Two modes:
 - «Drift» CAM: 1 dV (explicit formula) consists in creating a drift between Mango and Tango
 - «Soft» CAM : 2 dV (explicit formulas) aims at setting the main spacecraft onto a stable relative orbit around the target (radial and normal separations phased in quadrature)

Nominal Mission: CAM operations «Drift» CAM 1 dV

Fictitious or Real Target	Target position (m)	KOZ threshold (m)	Duration free drift (orbits)	Delta-V consumption (cm/s)	KOZ criteria
Fictitious	[90 0 0]	22	6.7	3.9	Ok
Real	[0 0 0]	22	8.3	3.8	Ok
	[0 0 0]	40	7.0	8.0	Ok
	[0 0 0]	45	6	10.5	Ok

- ♦ All «drift» CA successfully executed
- ♦ Exiting Keep out Zone a few seconds after CA maneuver



Potential risk of this strategy

- ♦ Weak drift on X_{slo}
- ♦ Projection onto the $\{Y, Z\}_{slo}$ plan \neq circle whose radius = KoZ threshold

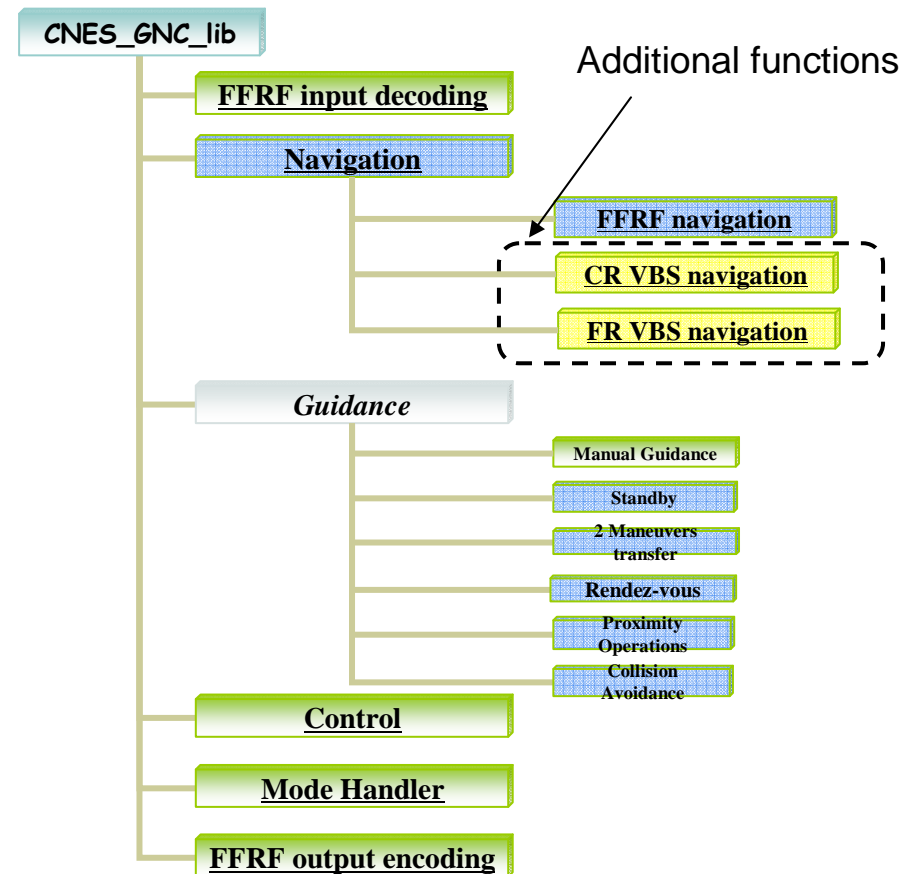
Summary

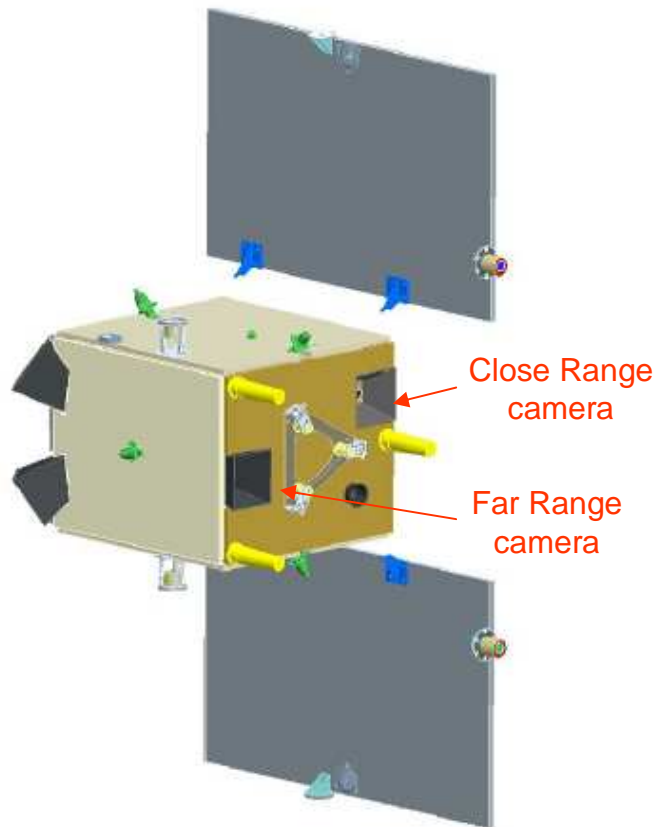
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- Extended mission
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 - ♦ Results synthesis
- GNC results summary



Extended mission GNC Software: GNC functions overview

- 2 new navigation functions integrated within CNES_GNC_lib to process VBS measurements
- 1 guidance function (2 MT) programmed differently to allow guidance via waypoints





Short range camera:

- works in cooperative mode at short range ($d < 50$ m)
 - relies on IR LEDs activation on Target satellite
- determines @ 1 Hz Target relative position and orientation by comparing the diodes pattern with the model stored in database
- CNES will only use the position measurement

Far range camera:

- Customized star tracker that can detect orbital objects
- Detection of an orbital object is made by comparison with the star catalogue and analysis of the apparent motion (→ brightest object only)
- Tracks the target and delivers its direction angles along with the camera inertial attitude
- *Basic image processing performed at short range ??*

GNC Activity	Number of occurrences	Duration
Metrology transition	1 open loop session 3 closed loop sessions	4 days
Vision based rendezvous	1 open loop session 3 closed loop sessions	4 days
Vision based relative orbit keeping	1 session	0,5 days

8,5 jours de boucle fermée
4.8 m/s delta-V
3 à 4 changements de mode par jour

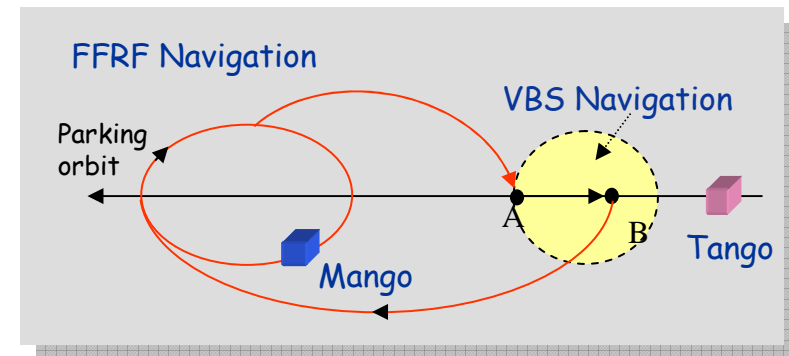
POD-DLR (Precise Orbit Determination)
are used as reference for performance
evaluation

■ Function : Determination of MANGO relative state using CR VBS data

- ◆ EKF to estimate up to 8 states : 3 for position, 3 for position rate and optionally 2 for the VBS direction biases
- ◆ Adaptation of the FFRF navigation filter for the processing of slightly different measurements (3D position set converted into distance and direction angles)
- ◆ Tango Local orbital frame obtained by propagation (as for FFRF navigation)
- ◆ Developed in C code

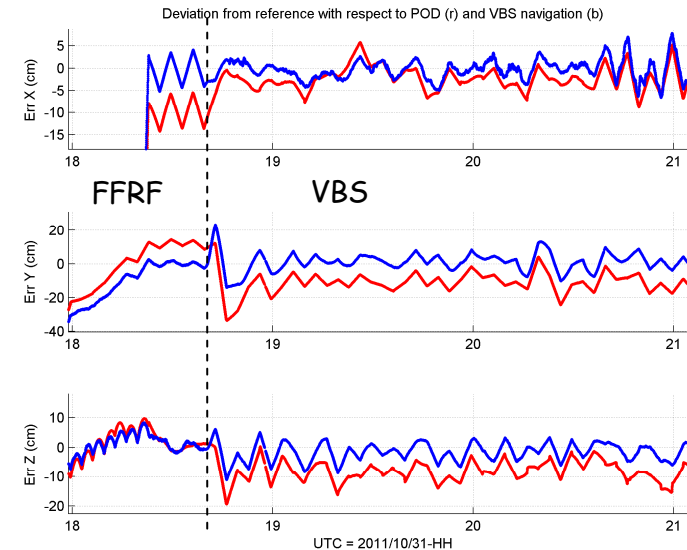
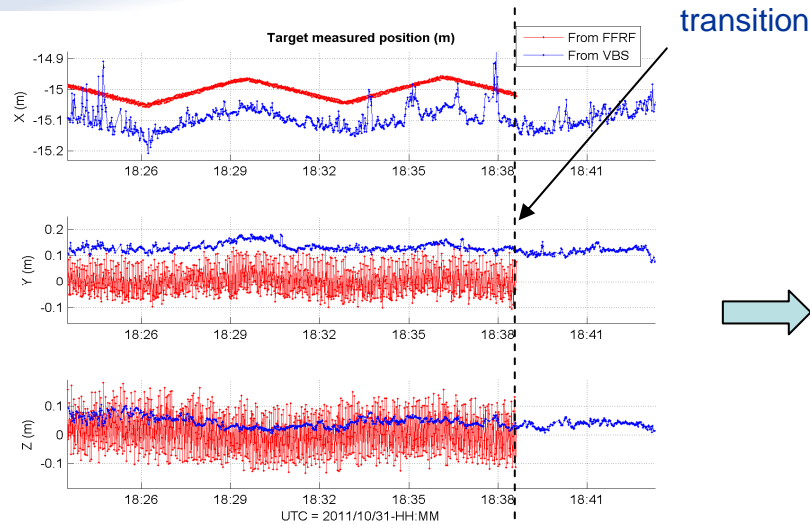
➔ This function allows to exercise metrology transitions: FFRF -> VBS and VBS -> FFRF and test proximity control performance

➔ A similar function is available in PRISMA and can be used in FFIORD loop for performance comparison



Extended mission GNC results

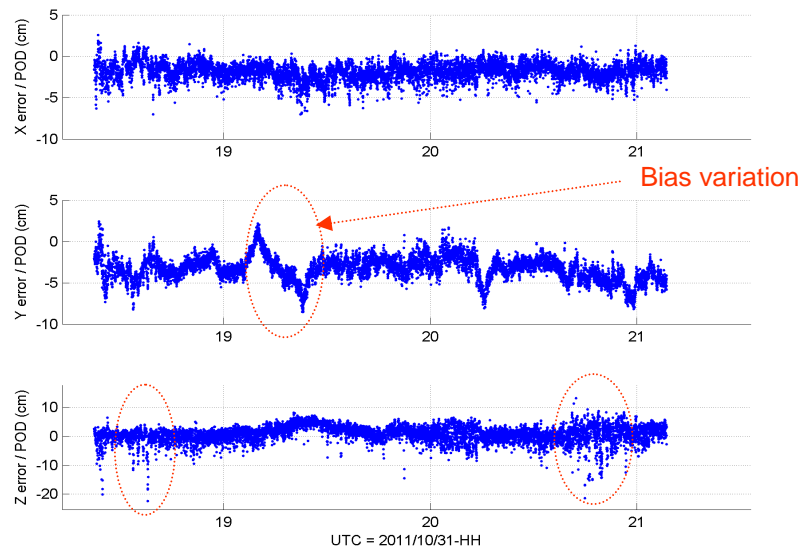
Proximity operations with metrology transition (1)



- 4 transition experiments were performed with a satisfactory functional behaviour
- Distance errors affect the navigation performance and control accuracy is not improved w.r.t. FFRF navigation
- Control strategy is to be tailored to reduce navigation stress (to be relaxed before and during transition phase)

Experiment	Navigation error (cm) POD as ref	Control error (cm) VBS nav as ref	Control error (cm) POD as ref
PROX @ 15 m (OHB nav)	Bias [0.8 2.4 3.1] Std [5.6 1.4 1.2]	Bias [2.8 0.1 0.1] Std [14 4.4 5.3]	Bias [4.1 2.4 2.9] Std [14 4.5 5.2]
PROX @ 15 m (CNES nav)	Bias [2.0 12 6.4] Std [1.9 3.8 2.0]	Bias [0.2 1.1 1.6] Std [2.2 5.3 2.9]	Bias [2.2 11 8.2] Std [2.5 6.0 3.3]

VBS measurement error (POD reference)



Target satellite at 15 m distance



VBS measurements suffer from temporary noise increase (distance) and bias variations that affect control performance (LED detection perturbed by optical artefacts)

- ➔ Positioning stability could not reach the level obtained with FFRF measurements even through ground replay tests
- ➔ High performance is achievable but requires cleaner optical conditions (robustness of the optical target detection to be improved)

■ Navigation Function : estimation of MANGO relative state using FR VBS data

- Distance is not available but can be observed in presence of manoeuvres applied along the rendezvous trajectory
- Based on an Extended Kalman Filter with 6 states : 3 for position, 3 for position rate
- Dynamic model: Yamanaka Ankersen formulation
- Automatic tuning of filter parameters (scheduling depending on relative range)

■ Navigation Characteristics

- ♦ Simulink implementation
- ♦ Development by TAS Cannes (R&T) and encapsulated by CNES
- ♦ Performance very dependent on guidance strategy (manoeuvres direction and amplitude) and relative range initial uncertainty

■ Guidance function

- ♦ Implementation of a waypoint oriented strategy using an already available algorithm (multiple manoeuvre transfer) with a different programming method



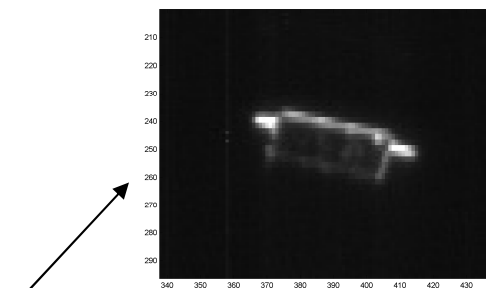
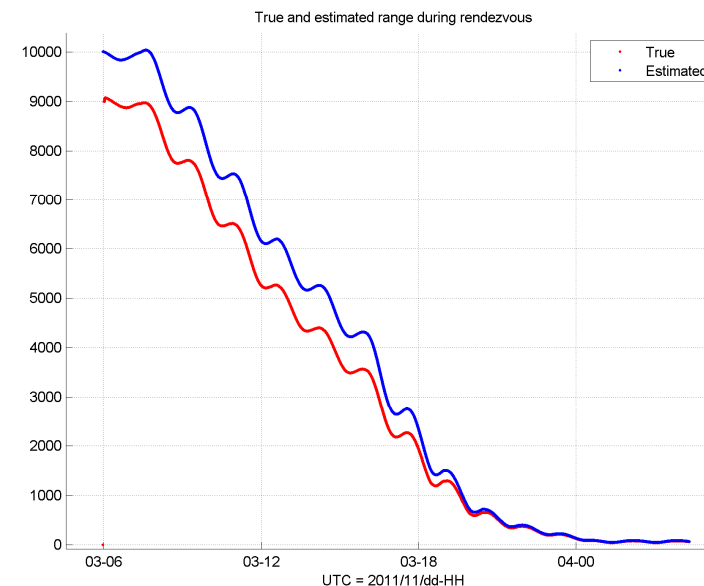
Extended mission GNC results

Angles only navigation (1)

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Experiment	Duration (hours)	Range accuracy (%)	Expected Delta V (cm/s)	Real Delta V (cm/s)
RdV 4 km to 100 m (OL)	16.2	1.8%	N/A	N/A
RdV 4 km to 100 m (CL)	16.2	2%	54.0	42.6
RdV 10 km to 100 m (CL)	18.5	3 %	98.5	86.8
RdV 10 km to 50 m (CL)	19.5	5.5%	74.0	73.6

- 4 RDV achieved successfully
- Satisfactory VBS behaviour at long and medium range (target detection and tracking)
- Range uncertainty reduction is not significant above 2 km
- Limited range accuracy at short range due to the target direction uncertainty



target size > 40 pixels at 50 m

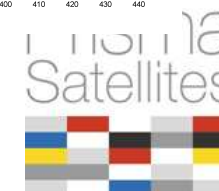
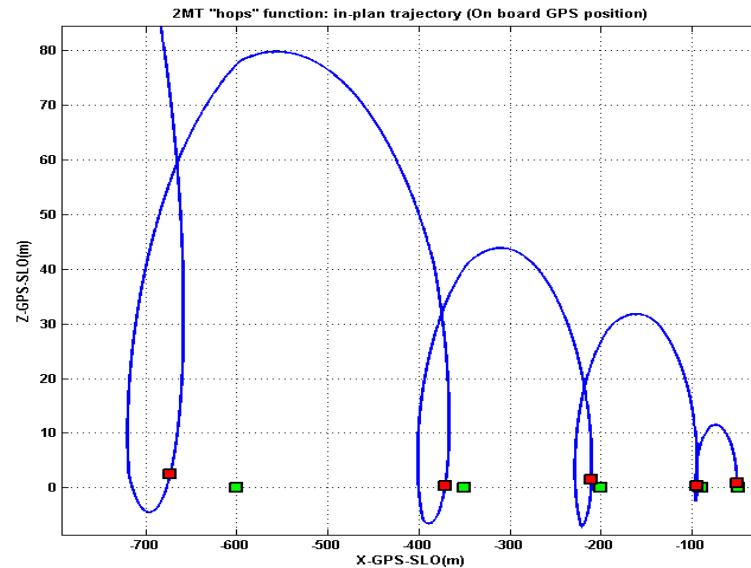
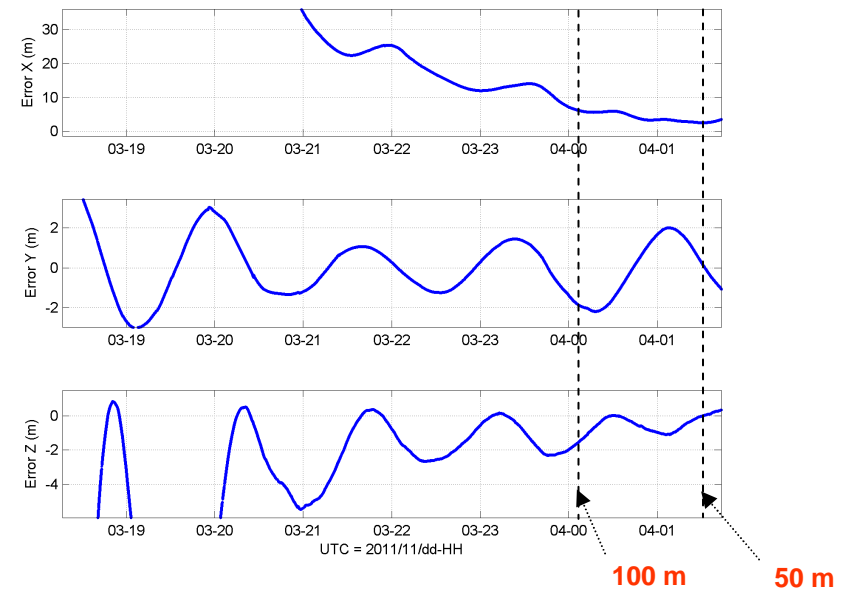


Illustration of waypoint oriented guidance



Performance at short range



- Difficulty to reduce relative range uncertainty at long distance at a reasonable cost
- Performance improvement at short range is achievable with some basic image processing (outside the VBS)

■ FFRF based activities

- ♦ **All RDV and FF activities were successfully demonstrated**
 - sensor & algorithm integrated behavior showed a great robustness → complex sequences were routinely performed (autonomy) with the expected performance level
- ♦ **Short range positioning was achieved with a high stability (a few cm)**
 - positioning performance exceeds requirements for a first stage metrology

■ VBS based activities

- ♦ **RDV based on Angles-only navigation was demonstrated several times**
 - VBS showed a satisfactory robustness at all ranges
 - Navigation performance at short range can be improved by image processing implemented in the OBC (not possible on PRISMA)
- ♦ **Metrology transition / VBS based control was exercised several times**
 - Allowed to evaluate the transition issues in terms of navigation and control performance
 - VBS behavior was satisfactory but measurement performance was not sufficient to demonstrate a higher positioning accuracy → high performance requires a better robustness of the target identification process

